

# Optimized parameters for Tuyen Quang reservoir basin using HEC-HMS model

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**Abstract**— In the calculation of discharge into hydroelectric reservoirs, the calibration and verification of the hydrological model HEC-HMS by trial process takes a long time and the found parameters is not optimal. This paper presents the results of using the Trial Optimal feature in the HEC-HMS to automatically detect the optimal set of parameters, calculate the inflow to Tuyen Quang reservoir. At first, the values of parameters are automatically assigned to the model. Then, HEC-HMS uses the Trial Optimal feature to detect the optimal parameters through iterative and selective calculation based on the observed data. The optimal parameters are applied to simulate the inlet discharge from May 23, 2022 to May 31, 2022 and verified the discharge from June 10, 2022 to June 17, 2022. The calculation results, that are estimated the accuracy by NSE index, show that the Trial Optimal feature has made the process of detecting the optimal parameters more accurate.

**Keywords**— HEC-HMS, Optimal, Tuyen Quang reservoir.

## I. INTRODUCTION OF HEC - HMS

HEC-HMS is a product of the Hydrologic Engineering Center within the U.S. Army Corps of Engineers. It is designed to simulate the precipitation-runoff processes of drainage basins. That can be applicable in a wide range of geographic areas for solving the widest possible range of problems. Including flood hydrology, natural watershed runoff ,...

The program is capable of representing many different watersheds. A model of the watershed is constructed by separating the water cycle into manageable pieces and constructing boundaries around the watershed of interest. Any mass or energy flux in the cycle can then be represented with a mathematical model. In most cases, several model choices are available for representing each flux. Each mathematical model included in the program is suitable in different environments and under different conditions. Making the correct choice requires knowledge of the watershed, the goals of the hydrologic study, and engineering judgement.

In HEC-HMS observed data can be used to optimize model's performance by automatically estimating parameters. In this paper the authors used two different approaches in HEC- HMS optimization: Simplex and Differential Evolution (DE). Simplex method starts with given initial parameters and adjusts them so that the simulation results match the observed data as closely as

possible. Differential Evolution generates set of parameters and deals with uncertain parameters. Differential Evolution uses mutation as a search mechanism and selection to direct the search toward the prospective regions in the feasible region. It will result in different parameter sets with each experiment.

### A. Simplex optimal

Simplex searches for the optimal parameter value without using derivatives of the objective function to guide the search. Instead this algorithm relies on a simpler direct search. In this search, parameter estimates are selected with a strategy that uses knowledge gained in prior iterations to identify good estimates, to reject bad estimates, and to generate better estimates from the pattern established by the good.

The simplex search uses a simplex - a set of alternative parameter values. For a model with  $n$  parameters, the simplex has  $n+1$  different sets of parameters.

For example, if the model has two parameters, a set of three estimates of each of the two parameters is included in the simplex. Geometrically, the  $n$  model parameters can be visualized as dimensions in space, the simplex as a polyhedron in the  $n$ -dimensional space, and each set of parameters as one of the  $n+1$  vertices of the polyhedron. In the case of the two-parameter model, then, the simplex is a triangle in two-dimensional space, as illustrated in "Fig. 1".

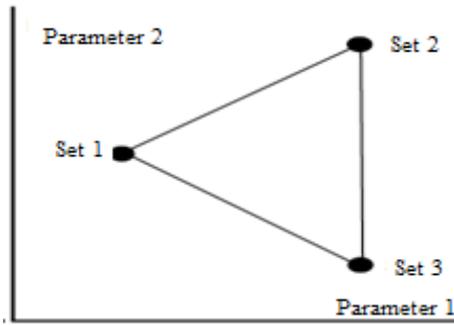
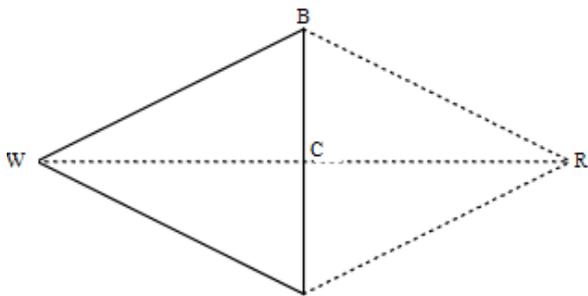


Fig. 1. Initial simplex for a 2-parameter model

This method is to find a vertex at which the value of the objective function is a minimum. To do so, it uses the following operations:

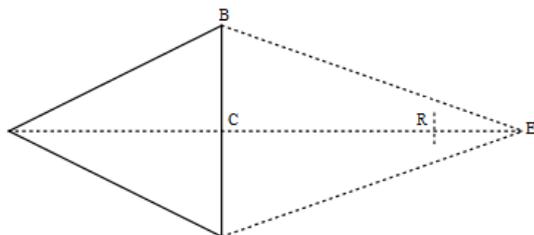
- **Comparison:** The first step in the evolution is to find the vertex of the simplex that yields the worst (greatest) value of the objective function and the vertex that yields the best (least) value of the objective function. In “Fig. 2”, these are labeled W and B, respectively.
- **Reflection:** The next step is to find the centroid of all vertices, excluding vertex W; this centroid is labeled C in “Fig. 2”. The algorithm then defines a line from W, through the centroid, and reflects a distance WC along the line to define a new vertex R, as illustrated “Fig. 2”.



$$x_i (\text{reflected}) = x_i (\text{centroid}) + 1.0 [x_i (\text{centroid}) - x_i (\text{worst})]$$

Fig. 2. Reflection of a simplex

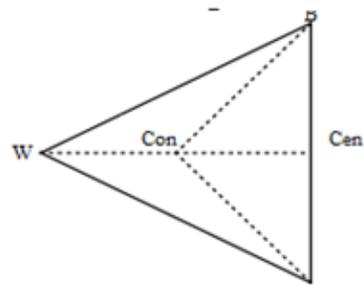
- **Expansion:** If the parameter set represented by vertex R is better than, or as good as, the best vertex, the algorithm further expands the simplex in the same direction, as illustrated in “Fig. 3”. This defines an expanded vertex, labeled E in the figure. If the expanded vertex is better than the best, the worst vertex of the simplex is replaced with the expanded vertex. If the expanded vertex is not better than the best, the worst vertex is replaced with the reflected vertex.



$$x_i (\text{expanded}) = x_i + 2.0 [x_i (\text{reflected}) - x_i (\text{centroid})]$$

Fig. 3. Expansion of a simplex

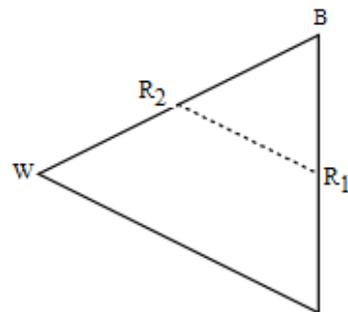
- **Contraction:** If the reflected vertex is worse than the best vertex, but better than some other vertex (excluding the worst), the simplex is contracted by replacing the worst vertex with the reflected vertex. If the reflected vertex is not better than any other, excluding the worst, the simplex is contracted. This is illustrated in “Fig. 4”. To do so, the worst vertex is shifted along the line toward the centroid. If the objective function for this contracted vertex is better, the worst vertex is replaced with this vertex.



$$x_i (\text{contracted}) = x_i (\text{centroid}) - 0.5 [x_i (\text{centroid}) - x_i (\text{worst})]$$

Fig. 4. Contraction of a simplex

- **Reduction:** If the contracted vertex is not an improvement, the simplex is reduced by moving all vertices toward the best vertex. This yields new vertices R<sub>1</sub> and R<sub>2</sub>, as shown in “Fig. 5”.



$$x_{ij} (\text{reduced}) = x_i (\text{best}) + 0.5 [x_{ij} - x_i (\text{best})]$$

Fig. 5. Reduction of a simplex

The search terminates when either of the following criterion is satisfied:

$$\sqrt{\sum_{j=1, j \neq \text{worst}}^n \frac{(z_j - z_c)^2}{n-1}} < \text{tolerance}$$

In which: n = number of parameters; j = index of a vertex, c = index of centroid vertex; and z<sub>j</sub> and z<sub>c</sub> = objective function values for vertices j and c, respectively.

Or the number of iterations reaches 50 times the number of parameters.

The parameters represented by the best vertex when the search terminates are reported as the optimal parameter values [1].

### B. Differential evolution optimal

DE is a population based search technique which utilizes NP variables as population of D dimensional parameter



TABLE I. MAIN PARAMETERS

Parameter	Unit	Value
Green and Ampt - Conductivity	mm/hr	0.4
Green and Ampt - Suction Scale Factor		0.6
Green and Ampt - Initial Content Scale Factor		0.8
Green and Ampt - Saturated Content Scale Factor		0.9
SCS Unit Hydrograph	minute	570
Routing - Lag - Initial Discharge	m <sup>3</sup> / s	5
Routing - Lag	minute	200

The basin is divided into 15 basins and 7 reaches, the total number of parameters that used to be adjusted is 82. The initial values of the parameters are estimated as follow:

- Water concentration time in the basin ( $T_c$ ) and water storage coefficient in the basin ( $R$ ) are calculated according to the length of the main river from the source to the outlet of the basin, the length from the outlet to the center of the basin and the average slope of the flow path;
- Green and Ampt parameters are estimated from land cover and land use maps of the basin;
- Transmission time depends on the length and slope of the river branch.

The maximum and minimum value range of each parameter is selected corresponding to these initial values.

### III. SCENARIOS AND CALCULATION

Had the model established, the authors have simulated and calibrated the inflow discharge into Tuyen Quang reservoir with two different rain station assignment methods: Specified Station (SS) and Inverse Distance (ID) as shown in “Table II”:

TABLE II. SCENARIOS AND CALCULATION

Scenarios		SS	ID
Calibration 23/5/2022 30/5/2022	Calibration	PA1	PA2
	Simplex Optimal	PA3	PA4
	DE Optimal	PA5	PA6
Verification 10/6/2022 - 17/6/2022		PA7	PA8

The results of SS calibration and optimization are shown as “Fig. 7”:

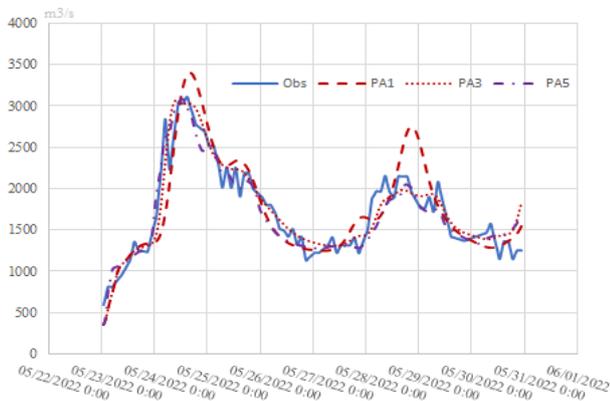


Fig. 7. SS calibration and optimization

The results of ID calibration and optimization are shown as “Fig. 8”:

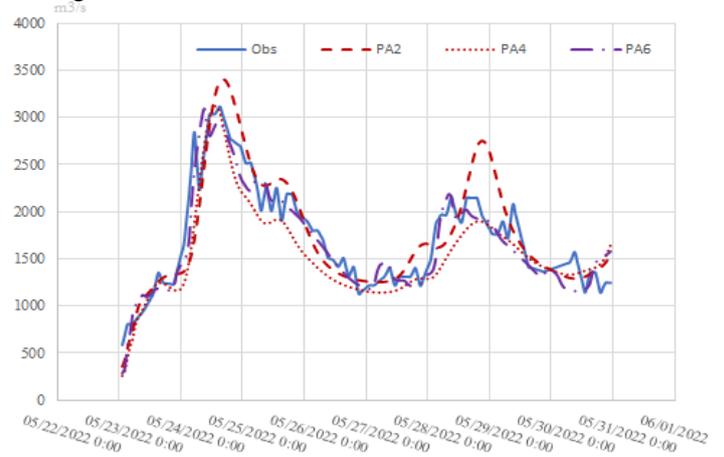


Fig. 8. ID calibration and optimization

The calculation results are evaluated using the NSE index (Table III).

TABLE III. NSE INDEX OF THE RESULTS

Scenarios	SS	ID
Calibration	0.80	0.77
Simplex Optimal	0.91	0.92
DE Optimal	0.91	0.94

Although calculation time of each calibration is short, but achieving the best final result requires trial and error many times and depends on the experience of the forecaster. In addition to reducing time of calculation, Optimal also provides outstanding results as the NSE index above. Notice that the calculation time of the Simplex algorithm only reaches 1/3 calculation time of the DE algorithm, but the NSE index results are not as good as.

The NSE index shows that DE optimal yield the best results. Using the set of DE optimal parameters that obtained after calibration, the authors have verified the model (PA7, PA8) as “Fig. 9”.

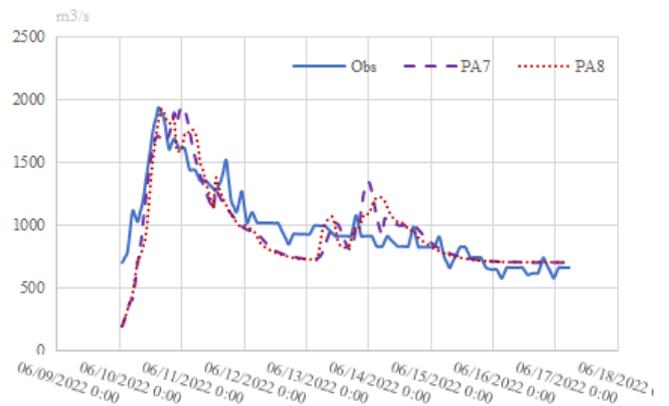


Fig. 9. Verification results

Verification results are evaluated by the NSE index, the SS verification NSE = 0.66, DI verification NSE = 0.67. This shows that the parameters obtained in the calibration accurately and reflects the characteristics of the basin. The NSE value of the verification are good.

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For a deeper evaluation of the DE optimal method, the authors calculated additional options with different parameters. Then apply the optimized value of the parameters to validate the model. “Tables IV, V” are the results of DE optimal with different parameters.

TABLE IV. DE OPTIMAL WITH DIFFERENT ITERATIONS

Population size 30								
Ite	20	50	100	200	300	400	500	900
NSE	0.166	0.753	0.937	0.928	0.927	0.820	0.813	0.801

TABLE V. DE OPTIMAL WITH DIFFERENT POLULATION SIZES

Iteration 100								
Size	10	20	30	40	50	60	70	80
NSE	-1.10	0.896	0.937	0.945	0.939	0.930	0.935	0.922

It is noticed that when the population size is 30 or more, the NSE value has reached around the maximum level (NSE  $\approx$  0.94). The difference in NSE value is due to the random selection of initial values. If these random values are closer to the maximum value (easier to reach the optimal solution), NSE will achieve better results.

The result shows that, corresponding 82 parameters that need to be adjusted, the Tuyen Quang basin only needs a population size of 40 and 100 iterations to get the best result of DE optimal. This number of parameters is reasonable for Tuyen Quang basin as well as a reference for other basins.

## IV. CONCLUSION

Calculation results show that the parameter optimization feature in the HEC-HMS hydrological model greatly helps in finding optimal parameters for model calibration.

For the Tuyen Quang basin, the DE algorithm has higher accuracy but the running time is longer than the Simplex algorithm. DE algorithm, for the Tuyen Quang basin divided into 15 sub-basins), gives the best result when population size is 40 in 100 iterations.

Calculating scenarios using the algorithm to automatically detect optimal parameters brings many benefits and helps forecasters gain more experience to apply to the Tuyen Quang basin as well as other basins.

## ACKNOWLEDGMENT

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